

# Asreml-R: an R package for mixed models using residual maximum likelihood

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# Outline

- 1 Introduction
- 2 The linear model
  - Specifying the linear model in asreml-R
  - The asreml class
- 3 An example
  - Models for a series of trials

# Introduction

- **ASReml**: standalone program (Gilmour *et al.*, 1999)
- Designed to fit complex mixed models to large problems.
- Efficient computing strategies
  - Average Information algorithm (Gilmour *et al.*, 1995)
    - avoids forming expensive trace terms
  - Sparse matrix methods
    - avoid forming and storing zero cells
    - exploit variance structures with sparse inverses
    - optimize solution order
  - Direct product structures exploited
    - $(\mathbf{A} \otimes \mathbf{B})^{-1} = \mathbf{A}^{-1} \otimes \mathbf{B}^{-1}$

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# Asreml-R

- asreml-R is the R interface to the ASReml fitting routines.
- model specified as formula objects
- initial values specified as list objects
- asreml object
  - BLUPs of random effects
  - GLS estimates of fixed effects
  - REML estimates of variance components
  - predictions from the linear model (if requested)

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# The linear model

$$\mathbf{y} = \mathbf{X}\boldsymbol{\tau} + \mathbf{Z}\mathbf{u} + \mathbf{e}$$

- $\mathbf{y}$  denotes the  $n \times 1$  vector of observations
- $\boldsymbol{\tau}$  is a  $p \times 1$  vector of fixed treatment effects
- $\mathbf{X}$  is a  $n \times p$  design matrix
- $\mathbf{u}$  is a  $q \times 1$  vector of random effects
- $\mathbf{Z}$  is a  $n \times q$  design matrix
- $\mathbf{e}$  is a  $n \times 1$  vector of residual errors

# The linear model

$$\begin{bmatrix} \mathbf{u} \\ \mathbf{e} \end{bmatrix} \sim N \left( \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}, \theta \begin{bmatrix} \mathbf{G}(\boldsymbol{\gamma}) & \mathbf{0} \\ \mathbf{0} & \mathbf{R}(\boldsymbol{\phi}) \end{bmatrix} \right)$$

- Where:
  - $\mathbf{G}, \mathbf{R}$  parameterized variance matrices
  - $\boldsymbol{\gamma}$  a vector of variance parameters relating to  $\mathbf{u}$
  - $\boldsymbol{\phi}$  a vector of variance parameters relating to  $\mathbf{e}$
  - $\theta$  is a scale parameter
- $\mathbf{y} \sim N(\mathbf{X}\boldsymbol{\tau}, \mathbf{H})$
- $\mathbf{H} = \mathbf{R} + \mathbf{Z}\mathbf{G}\mathbf{Z}'$ .

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# Variance structures for the errors

## R structures

- $R$  may comprise  $t$  independent sections

$$R = \bigoplus_{j=1}^t R_j = \begin{bmatrix} R_1 & 0 & \dots & 0 \\ 0 & R_2 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & R_t \end{bmatrix}$$

- Each section may be the direct product of two or more dimensions

$$R_i = R_{i_1} \otimes R_{i_2} \otimes \dots$$

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# Variance of the random effects

## G structures

- The vector of random effects is often composed of  $b$  subvectors

$$\mathbf{u} = [\mathbf{u}'_1 \ \mathbf{u}'_2 \ \dots \ \mathbf{u}'_b]'$$

- The  $\mathbf{u}_i$  are assumed  $N(\mathbf{0}, \theta \mathbf{G}_i)$ .
- As for  $R$

$$\mathbf{G} = \bigoplus_{i=1}^b \mathbf{G}_i = \begin{bmatrix} \mathbf{G}_1 & 0 & \dots & 0 \\ 0 & \mathbf{G}_2 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \mathbf{G}_b \end{bmatrix}$$

- Assuming separability  $\mathbf{G}_i = \mathbf{G}_{i1} \otimes \mathbf{G}_{i2} \otimes \dots \otimes \mathbf{G}_{if}$

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# Specifying the linear model

*fit.asr <- asreml (fixed=, random=, rcov=, data=)*

- Fixed effects  
*fixed = y ~ model formula*
- Random effects (G structures)  
*random = ~ model formula*
- Error model (R structures)  
*rcov = ~ model formula*
- Sparse fixed  
*sparse = ~ model formula*  
Variance matrix for solutions not available
- Factors crossed or nested - determined by coding.
- *y* may be a matrix

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# Specifying variance models

## G structures

- The default variance model is (scaled) identity.
- Variance models for random terms are specified using *special functions*.
- For example

`random = ~ diag(A):B`

specifies a diagonal variance structure of order `length(levels(A))` for *A* and a (default) identity for *B*.

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- Default  $\sigma^2 I_n$ , where  $n < -\text{nrow}(\text{data})$
- Specified using *special functions*.
- Example: a series of  $t$  independent experiments indexed by the factor *Trial*,

```
rcov = ~ at(Trial):ar1(A):ar1(B)
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specifies separable autoregressive processes across  $A$  and  $B$  at each level of *Trial*

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# Special Functions

## Model functions

lin(obj=x)

Includes the named factor as a variate.

spl(obj=x)

Spline **random** factor.

pol(obj=x, t)

Orthogonal polynomials of order  $|t|$ .

## Time series type models

ar1(), ar2()

Autoregressive

ma1(), ma2()

Moving average

## Metric based models in $\mathcal{R}$ or $\mathcal{R}^2$

exp(), gau()

One dimensional

aexp(), agau()

Anisotropic 2D

mtrn()

Matérn class

## General structure models

cor(), corb(), corg()

Correlation

diag(), us(), ante(), chol()

Variance

fa(obj=x, q)

Factor Analytic with  $q$  factors

## Known structures

ped(), giv()

Use known inverse matrices.

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# The asreml class

Component	Description
loglik	log likelihood at termination
gammas	vector of variance parameter estimates
coefficients	list of fixed, random and sparse coefficients
vcoeff	variance of the coefficients
fitted.values	fitted values
residuals	residuals
sigma2	residual variance
predictions	list of predictions if specified
G.param	list object of variance models for random terms
R.param	list object of variance models for error term

## asreml methods

- `coef()` List with components *fixed*, *random* and *sparse*.
- `resid()` Vector of residuals.
- `fitted()` Vector of fitted values.
- `summary()` List including the `asreml()` call, REML log-likelihood, variance parameters, coefficients, residuals and components of  $\mathbf{C}^{-1}$  if requested.
- `wald()` A table of Wald tests for each fixed term.
- `plot()` Residual plots including the sample variogram, distribution, fitted values and trend plots.
- `predict()` Predictions from the linear model (eg, tables of adjusted means). See Gilmour *et al.* (2004) and Welham *et al.* (2004).

## Example: Multi-environment trials

In the context of a plant genetic improvement program,

- It is important to know how genotype performance varies with a change in environment, that is, to investigate ( $G \times E$ ) interaction.
- Identify genotypes with broad or specific adaptation.
- $G \times E$  is assessed in a series of designed experiments in a range of environments (METs)
- Environments may be geographic locations and/or years
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# Example: Mixed model for MET data

$$\mathbf{y} = \mathbf{X}\boldsymbol{\tau} + \mathbf{Z}_g\mathbf{u}_g + \mathbf{Z}_o\mathbf{u}_o + \mathbf{e}$$

- Assume  $\text{var}(\mathbf{u}_g) = \mathbf{G}_g = \mathbf{G}_e \otimes \mathbf{I}_g$
- $\mathbf{G}_e$  is the genetic variance matrix:

$$\mathbf{G}_e = \begin{bmatrix} \sigma_{g_1}^2 & \sigma_{g_{12}} & \sigma_{g_{13}} & \cdots & \sigma_{g_{1t}} \\ & \sigma_{g_2}^2 & \sigma_{g_{23}} & \cdots & \sigma_{g_{2t}} \\ & & \sigma_{g_3}^2 & \cdots & \sigma_{g_{3t}} \\ & & & \ddots & \\ & & & & \sigma_{g_t}^2 \end{bmatrix}$$

- Allow separate spatial covariance structures for the errors for each trial

$$\mathbf{R}_j = \sigma_j^2 \mathbf{R}_{c_j}(\phi_{c_j}) \otimes \mathbf{R}_{r_j}(\phi_{r_j})$$

## Example: METs in ASReml-R

```
asreml(yield ~ trial + ...,  
       random = ~ us(trial):genotype + ...,  
       rcov = ~ at(trial):ar1(column):ar1(row), ...)
```

- *trial* is a (fixed) factor with  $t$  levels
- *genotype* is a (random) factor with  $g$  levels
- `us(trial):genotype` models genotype effects in each trial with variance  $\mathbf{G}_e \otimes \mathbf{I}_g$  where  $\mathbf{G}_e$  is an **unstructured** form
- `at(trial):ar1(column):ar1(row)` models the residual effects for each trial with an  $\text{AR1} \times \text{AR1}$  correlation structure.

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# MET data set

- Stage 2 trials taken from the Qld barley program (Kelly *et al.*, 2007)
- 14 environments over 2 years of trialling: 2003/4
- 1255 unique genotypes tested
  - 698 in 2003
  - 720 in 2004
  - 163 genotypes common across years
- Partially replicated designs (Cullis *et al.*, 2006)
- Response variate is **grain yield**
- Pedigrees traced back four generations

# Analysis strategy

- 1 Initial spatial model for each experiment
  - analyse each trial separately, or
  - joint analysis with a diagonal variance model

```
qb.asr1 <- asreml(yield ~ Site,  
                 random = ~ diag(Site):Genotype,  
                 rcov = ~ at(Site):ar1(Column):ar1(Row),  
                 data = qb)
```

17,663 equations

56 variance parameters

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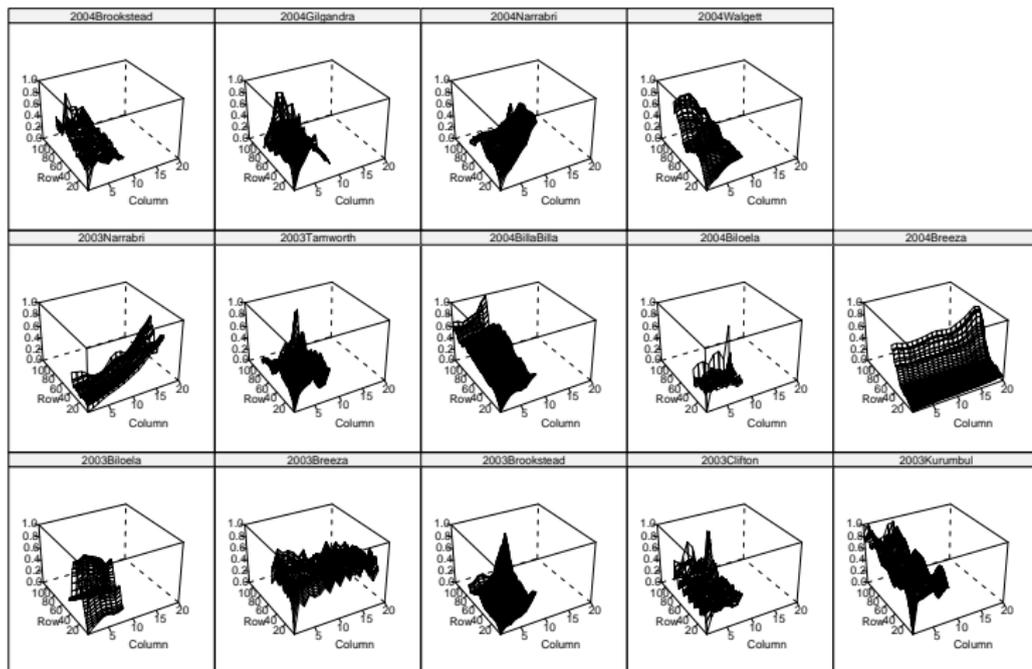
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`plot(qb.asr1,option='v')`



# Models for $G \times E$

- Diagonal variance structure analagous to individual analyses.
- Assumes that the genetic effects in different environments are un-correlated. Unlikely to be sensible.
- The `us()` model is the most general form for  $G_e$ . Difficulties:
  - With many environments, the number of parameters is large
  - Difficult to fit REML estimate of matrix can be **singular** - not full rank
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# Known genetic effects

- A better genetic variance model most likely achieved by partitioning genetic effects into **additive** and **non-additive**.
- If  $\mathbf{u}_g = \mathbf{a}_g + \mathbf{i}_g$ , then
  - Assume  $\mathbf{a}_g \sim N(\mathbf{0}, \sigma_a^2 \mathbf{A})$
  - Assume  $\mathbf{i}_g \sim N(\mathbf{0}, \sigma_i^2 \mathbf{I})$
  - $\text{var}(\mathbf{u}_g) = \mathbf{G}_{ae} \otimes \mathbf{A} + \mathbf{G}_{ie} \otimes \mathbf{I}$
- Asreml-R
  - 1 `ainv <- asreml.Ainverse(pedigree)$ginv`
  - 2 `asreml(..., ped(genotype), ... + ..., ide(genotype), ..., ginverse=list(genotype=ainv), ...)`

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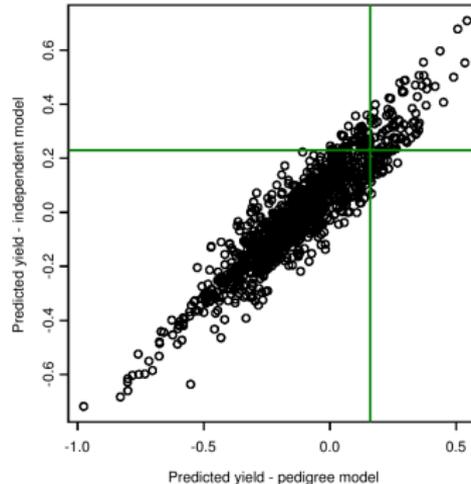
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# The final model

```
asreml(yield ~ Site+at(Site,c(3,6,8,13)):lincol + at(Site,c(3,8,10,11)):linrow +  
      at(Site,3):lincol:linrow + at(Site,4):fx4 + at(Site,6):fx6,  
      random = ~ fa(Site,3):ped(Genotype) + fa(Site):ide(Genotype) +  
      at(Site,c(2,4,5,7,9,11,12)):Column + at(Site,c(2)):Row,  
      rcov = ~ at(Site):ar1(Column):ar1(Row),  
      ginverse = list(Genotype=ainv), data=qb)
```

50,115 equations

134 parameters



# References

- Cullis, B., Smith, A., and Coombes, N. (2006). On the design of early generation variety trials with correlated data. *Journal of Agricultural, Biological and Environmental Statistics*, **(in press)**.
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